

1

[9].

n

(3), (4)

$$y = F(x_1, \dots, x_n), \quad (1)$$

$p_k, k = \overline{1, l},$

$$\tilde{F}(x_1, \dots, x_n) = \max, \quad (5)$$

$i(x_1, \dots, x_n) \leq b_i, i = \overline{1, m} \},$ (2)

$q_s, s = \overline{1, t},$

b_i

(1)

$\tilde{P}_k = [p_{k1}, p_{k2}], k = \overline{1, l},$

$$F(x_1, \dots, x_n) = \max, \quad (3)$$

$i(x_1, \dots, x_n) \leq b_i, i = \overline{1, m} \}.$ (4)

(3), (4)

$x^* = (x_1^*, \dots, x_n^*) (M = \{x^*\})$ (4),

$F_{\max}.$

(5), (6)

(3), (4),

$b_i, i = \overline{1, m}$

(3), (4).

$i, i = \overline{1, m}.$

(3),

(4) $F,$

i

b_i

$.1,$

(3), (4)

$(x', x''), x' = (x'_1, \dots, x'_n) -$

(3), (4), $x'' = (x''_1, \dots, x''_n) -$

(5), (6),

[5], $D(x', x'')$

$d.$

(3), (4).

2

[9],

$$\tilde{a} = [a_1, a_2], \tilde{b} = [b_1, b_2], \dots$$

$$\begin{aligned} \tilde{a} + \tilde{b} &= \{a + b \mid a \in \tilde{a}, b \in \tilde{b}\}, \tilde{a} - \tilde{b} = \\ &= \{a - b \mid a \in \tilde{a}, b \in \tilde{b}\}, k\tilde{a} = \{ka \mid a \in \tilde{a}\}, \dots \end{aligned} \quad (7)$$

$$\begin{aligned} [a_1, a_2] + [b_1, b_2] &= [a_1 + b_1, a_2 + b_2], \\ [a_1, a_2] - [b_1, b_2] &= [a_1 - b_1, a_2 - b_2]; \\ k[a_1, a_2] &= [ka_1, ka_2], k > 0, \\ &= [ka_2, ka_1], k < 0; \\ [a_1, a_2] \cdot [b_1, b_2] &= [\min_{i,j}(a_i \cdot b_j), \max_{i,j}(a_i \cdot b_j)]; \\ [a_1, a_2] / [b_1, b_2] &= [a_1 \cdot a_2] \cdot [1/b_2, 1/b_1]. \end{aligned} \quad (8)$$

$$[2, 8].$$

$$\tilde{a} = [a_1, a_2]$$

$$\tilde{b} = [b_1, b_2]$$

$$\tilde{a} \geq \tilde{b}$$

$$(a_i, b_j), \quad a_i \in \tilde{a}, b_j \in \tilde{b}.$$

$$\begin{aligned} (a_i, b_j) \\ a_i > b_j, \\ : a_i < b_j. \end{aligned} \quad (7).$$

$$a_1 \geq b_1, a_2 \geq b_2, \quad (10)$$

$$\tilde{a} \leq \tilde{b} -$$

$$a_1 \leq b_1, a_2 \leq b_2. \quad (11)$$

$$\tilde{b} = [b_1, b_2]$$

$$\tilde{a} = [a_1, a_2]$$

$$\tilde{a} \geq \tilde{b} \quad \tilde{a} \leq \tilde{b}$$

$$a_1, b_1$$

$$\tilde{a} \vee \tilde{b} = \{a \vee b \mid a \in \tilde{a}, b \in \tilde{b}\},$$

$$\tilde{a} \wedge \tilde{b} = \{a \wedge b \mid a \in \tilde{a}, b \in \tilde{b}\}. \quad (9)$$

$$\tilde{a} \tilde{b}, \quad (9),$$

$$a \quad b,$$

$$\tilde{a} \quad \tilde{b}.$$

$$(\tilde{a} \geq \tilde{b} \quad \tilde{a} \leq \tilde{b}), \quad : 1)$$

2.

$$\tilde{a} = [a_1, a_2] \quad \tilde{b} = [b_1, b_2], \dots$$

$$\tilde{a} \geq \tilde{b},$$

$$\tilde{a} \leq \tilde{b},$$

$$a_1 < b_1, a_2 > b_2 \quad b_1 < a_1, b_2 > a_2. \quad (12)$$

(12)

[10–12],

« »
2

(5), (6).

– , ,

[2, 8, 13].

(5), (6)

(

$\tilde{F}(x_1, \dots, x_n)$,

, , 1 2,

$\sim_{i, \overline{1, m}}$,

$\tilde{b}_i, i = \overline{1, m}$,

3.

$\tilde{a}(1)=[a_1(1), a_2(1)], \tilde{a}(2)=[a_1(2), a_2(2)], \dots$

(8), $\tilde{F} \sim_i$

\tilde{b}_i .

$$a_1(1) \geq a_1(2), a_1(1) \geq a_1(3), \dots;$$

$$\tilde{F}(x_1, \dots, x_n) = [F_1(x_1, \dots, x_n), F_2(x_1, \dots, x_n)],$$

$$a_2(1) \geq a_2(2), a_2(1) \geq a_2(3), \dots \quad (13)$$

$$\sim_i(x_1, \dots, x_n) = [_{i1}(x_1, \dots, x_n), _{i2}(x_1, \dots, x_n)], i = \overline{1, m}, \quad (15)$$

$$\tilde{b}_i = [b_{i1}, b_{i2}], \quad i = \overline{1, m}.$$

(13)

$\tilde{a}(1)$,

(5), (6)

4.

$\tilde{a}(1)=[a_1(1), a_2(1)], \tilde{a}(2)=[a_1(2), a_2(2)], \dots$

$$[F_1(x_1, \dots, x_n), F_2(x_1, \dots, x_n)] = \max, \quad (16)$$

$$[_{i1}(x_1, \dots, x_n), _{i2}(x_1, \dots, x_n)] \leq [b_{i1}, b_{i2}], i = \overline{1, m}. \quad (17)$$

$$a_1(1) \leq a_1(2), a_1(1) \leq a_1(3), \dots;$$

(16), (17)

$$a_2(1) \leq a_2(2), a_2(1) \leq a_2(3), \dots \quad (14)$$

$$(14), \quad (13),$$

(16)

$\tilde{a}(1)$,

3, 4

$$F_1(x_1, \dots, x_n) = \max, F_2(x_1, \dots, x_n) = \max. \quad (18)$$

()

(17)

3

$$_{i1}(x_1, \dots, x_n) \leq b_{i1}, \quad _{i2}(x_1, \dots, x_n) \leq b_{i2}, i = \overline{1, m}. \quad (19)$$

(18)

(3), (4)

(19),

(3), (4)

(3), (4)

(. . 2)

(5), (6)

$$F_1(x_1, \dots, x_n) = \max,$$

$$_{i1}(x_1, \dots, x_n) \leq b_{i1}, i = \overline{1, m},$$

(4)

(3),

$$_{i2}(x_1, \dots, x_n) \leq b_{i2}, i = \overline{1, m}, \quad (20)$$

$$F_2(x_1, \dots, x_n) = \max, \quad (21)$$

$$i_1(x_1, \dots, x_n) \leq \overline{b_{i1}}, \quad i = \overline{1, m},$$

$$i_2(x_1, \dots, x_n) \leq \overline{b_{i2}}, \quad i = \overline{1, m},$$

$$(5), (6). \quad (20) \quad (5), (6), \quad (8), \quad (3), (4), \quad (5), (6).$$

$$(21) - \quad (20) \quad (21) \quad (5), (6) \quad \tilde{F}, \quad \tilde{b}_i, i = \overline{1, m},$$

$$\{M(x), F_{1, \max}\}, \quad (5), (6) \quad (15).$$

$$\{M(x), F_{2, \max}\}. \quad (5), (6) \quad (20) \quad (21) -$$

$$M(x), M(x) - \quad \tilde{b}_i, i = \overline{1, m}, \quad (20) \quad (21) -$$

$$x = (x_1, \dots, x_n), \quad (5), (6).$$

$$F_{1, \max}, F_{2, \max} - \quad (20) \quad (21).$$

$$(5), (6) \quad 1, \quad (20) \quad (21).$$

$$\{x^* \in M(x) \cap M(x); \tilde{F}_{\max} = [F_{1, \max}, F_{2, \max}] \}. \quad (22)$$

$$(22), \quad (5), (6) \quad x^* \quad M(x) - \quad x \quad \{M(x), F_{1, \max}\}, \{M(x), F_{2, \max}\}, \quad M(x) -$$

$$6. \quad (20) \quad (21)$$

$$\tilde{F}_{\max} - \quad M(x), M(x).$$

$$F_{1, \max} \quad (3), (4)$$

$$F_{2, \max}. \quad (5), (6)$$

$$(5), (6) \quad (3), (4)$$

$$(3), (4) \quad (3), (4)$$

$$5. \quad 4$$

$$(3), (4)$$

$$; 2) \quad (5), (6), \quad (3), (4)$$

$$(3), (4), \quad ; 3)$$

$$(5), (6) \quad (3), (4) \quad (\dots 2)$$

$$5 \quad (x', x'')$$

$$(\quad) \quad x' = (x'_1, \dots, x'_n) - \quad (3), (4), \quad x'' = (x''_1, \dots, x''_n) -$$

$$1. \quad (3), (4), \quad (5), (6),$$

$$(\quad) \quad D(x', x'')$$

$$[10-12], \quad x' = (x'_1, \dots, x'_n) \quad (3), (4). \quad d.$$

$$(\quad) \quad (3), (4)$$

1. 6-
 4, (3), (4)
 (3), (4)
 2.

2.
 $x' = (x'_1, \dots, x'_n)$ (3), (4),
 1.
 $x'' = (x''_1, \dots, x''_n)$
 (5), (6),
 (x', x'')

3.
 x', x''
 $D(x', x'')$
 $D(x', x'') = \sqrt{(x'_1 - x''_1)^2 + \dots + (x'_n - x''_n)^2}$ (23)

4.
 $D(x', x'')$
 d :
 $D(x', x'') \leq d$ (24)

(4)
 (24), (3),
 2,
 $x' = (x'_1, \dots, x'_n)$

(3), (4),
 1,
 $x'' = (x''_1, \dots, x''_n)$ (5), (6)
 1.
 (x', x'')
 (x', x'') , (24),
 (3), (4)

(3), (4)

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Levin V. I.

Dr. Sci., professor, Penza State Technological University, Russia

THE STABILITY OF SOLUTION OF SYSTEMS WITH UNDEFINED PARAMETERS OPTIMAL DESIGN PROBLEM

Our article considers the problem of optimization of incompletely specified functions, namely, functions which parameters are given within range of possible values. It is shown that solution of this problem also requires solving problem of determining stability of optimum of such functions to variation of values of their parameters. A method for obtaining such optimum of incompletely defined functions is presented. Method uses determination of problem. It allows to split original non-deterministic problem into two optimization problem of deterministic functions, which are solved separately. After that solutions are combined into one which is a solution of original problem. The article also provides a method for determining the stability of the optimum found of incompletely defined functions by methods of interval mathematics. We formulate 5 theorems determining the conditions for existence of optimum of incompletely defined function and its resistance to changing the function parameters. Algorithms for verifying the stability function are given

Keywords: system optimization, uncertainty, stability of optimum, variation of parameters, interval mathematics.

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